

## Application of the Capacitance-Voltage curve to photovoltaic cell characterizations

### I- Introduction

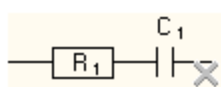
Capacitance measurement is widely used to carry out semiconductor characterization such as photovoltaic (PV) cells. For example, this measurement is used to determine the doping concentration.

In EC-Lab<sup>®</sup> & EC-Lab<sup>®</sup> Express software, it is possible to directly plot the capacitance (directly means without any post-process). The capacitance can be obtained with all the Electrochemical Impedance Spectroscopy (EIS) techniques *i.e.* Potentio EIS (PEIS), Galvano EIS (GEIS), Staircase PEIS (SPEIS), Staircase GEIS (SGEIS), "Wait" technique that allows user to follow up the modulus of Z vs time (PEISW) techniques.

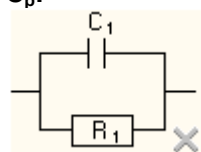
Depending on the model circuits considered, two types of capacitance,  $C_s$  or  $C_p$ , are calculated. The capacitance  $C_s$  corresponds to the capacitance of the R+C (in series) circuit and  $C_p$  corresponds to the capacitance of the R/C (in parallel) circuit (Fig. 1)

|              | X                                   | Y1                                  | Y2                       |
|--------------|-------------------------------------|-------------------------------------|--------------------------|
| freq/Hz      | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| Re[Z]/Ohm    | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| -Im[Z]/Ohm   | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| Z /Ohm       | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| Phase[Z]/deg | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| time/s       | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| <Ewe>/V      | <input checked="" type="checkbox"/> | <input type="checkbox"/>            | <input type="checkbox"/> |
| <I>/mA       | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| <b>Cs/μF</b> | <input type="checkbox"/>            | <input checked="" type="checkbox"/> | <input type="checkbox"/> |
| Cs-2/μF-2    | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| <b>Cp/μF</b> | <input type="checkbox"/>            | <input checked="" type="checkbox"/> | <input type="checkbox"/> |
| Cp-2/μF-2    | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |
| cycle number | <input type="checkbox"/>            | <input type="checkbox"/>            | <input type="checkbox"/> |

$C_s$ :



$C_p$ :



**Fig. 1: The two equivalent circuits offered for direct capacitance plotting.**

This note exhibits how to plot Capacitance vs. Voltage (C-V) curve. Firstly, the different options offered to plot the capacitance are shown with a varia-capacitor\* as an experimental model system. Selection of the circuit model and comparison between values of capacitance fitted with Zfit and the capacitance directly available in the technique are discussed. Secondly, typical C-V characterizations of PV cell are described.

\*capacitor whose capacitance may be intentionally and repeatedly changed mechanically or electronically

### II- Experimental conditions

Investigations are carried out with a SP-200 equipped with the Ultra Low Current option or with SP-300 and EC-Lab<sup>®</sup> software. For both systems (*i.e.* varia-capacitor and photovoltaic cell), investigations are done with a standard two-electrode connection.

The characteristic of the varia-capacitor is the following:

- low voltage variable capacitance double diode (BB201 from NXP).
- The capacitance is in the range of 10 to 120 pF for a voltage range of 0.5 to 11V.

The C-V characterization of the PV cell has been performed on a cell irradiated by a Xenon lamp of 150 W (light source of MOS-200 powered by ALX-150 power supply).

*Note: All settings and raw data files presented hereafter are available in the Data Sample folder of EC-Lab<sup>®</sup> Software as filename\_C\_V charact.mpr,*

### III- Varia-capacitor investigations

#### III-1. R/C or R+C equivalent circuit?

To choose the appropriate equivalent circuit among R/C or R+C, an EIS measurement on a wide frequency range *i.e.* 3 MHz to 1 mHz is performed. Settings are displayed in Fig. 2.

The EIS measurement leads to a semicircle (Fig. 3), so the R/C model ( $C_p$  variable) is considered for the C-V investigations.

The fitted values of R and C are 70 Ohm and 145 pF (Fig. 4), respectively.

The screenshot shows the settings for an EIS measurement. Key parameters include:

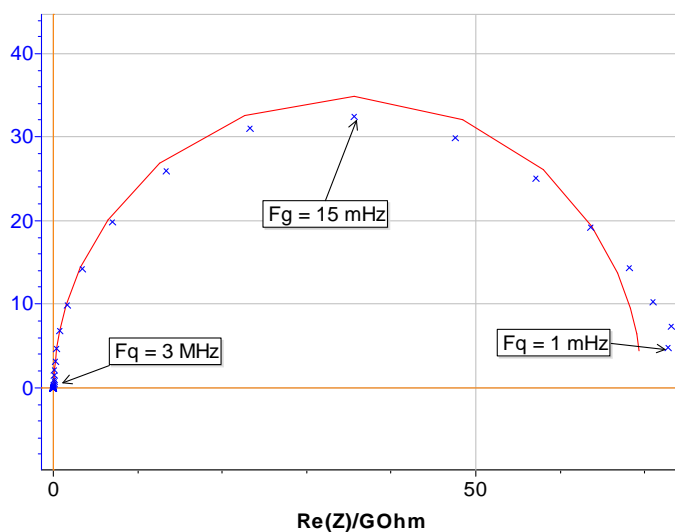
- Mode:** Single Sine (selected), Multi Sine.
- Set  $E_{we}$  to  $E$ :** 0,000 0 V vs.  $E_{oc}$ .
- for  $t_E$ :** 0 h 0 mn 0,000 s.
- Record every  $dI$ :** 0,000 mA.
- or  $dt$ :** 0,000 s.
- Scan from  $f_i$ :** 3,000 MHz.
- to  $f_f$ :** 1,000 mHz.
- with:**  $N_d = 6$  points per decade (selected), or  $N_T = 51$  points from  $f_i$  to  $f_f$ .
- in:** Logarithmic spacing (selected), or Linear spacing.
- sinus amplitude  $V_a$ :** 50,0 mV ( $V_{rms} \sim 35,36$  mV).
- wait for  $p_w$ :** 0,10 period before each frequency.
- average  $N_a$ :** 10 measure(s) per frequency.
- drift correction:** checked.
- Repeat  $n_c$ :** 0 time(s).
- E Range:** -10 V; 10 V. Resolution = 333,33  $\mu V$ .
- I Range:** Auto.
- Bandwidth:** 9 (~ 17h28mn / scan).

**Fig. 2: Settings for the EIS characterizations of the varia-capacitor.**

#### III-2 C-V investigations

Two SPEIS techniques are performed. One in the frequency range from 7 MHz to 1 Hz (setting displayed in Fig. 5) and one at one frequency (similar settings than shown in Fig. 5 with  $f_i$  equal to  $f_f$ ). Measurements are performed at a frequency of 323 kHz because above this frequency the responses of the

varia-capacitor is dependent on the frequency (Fig. 6). The experiments are named  $SPEIS_{7MHz-1Hz}$  and  $SPEIS_{323kHz}$ , respectively. The voltage scan starts at 0V and goes up to 10V with steps of 200 mV.



**Fig. 3: Nyquist plot of varia-capacitor (Exp data fitted data).**

The Z Fit software interface shows the following details:

- Equivalent circuit:** C1/R1.
- Table of parameters:**

| param. | sel.                                | sign | value      | unit | dev.      |
|--------|-------------------------------------|------|------------|------|-----------|
| C1     | <input checked="" type="checkbox"/> | +/-  | 0,145 8e-9 | F    | 3,689e-21 |
| R1     | <input checked="" type="checkbox"/> | +/-  | 69,75e9    | Ohm  | 0,349 4   |
- Calculate:**
  - Fit:** Select all cycle(s).
  - Method:** Randomize + Simplex.
  - Randomize:** all cycles.
  - Stop randomize on:** 10000 iterations.
  - Stop fit on:** 5000 iterations.
  - Weight:**  $\chi^2$ .
  - $\chi^2$ :** 0,020 96.
  - Iterations:** 5000 (Simplex) Cycle xxxx.

**Fig. 4: Values of the Zfit process.**

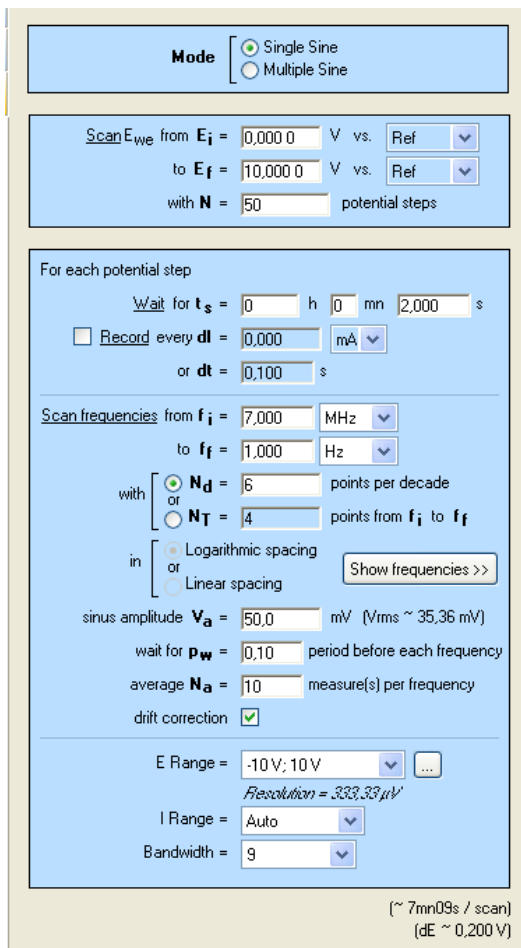


Fig. 5: SPEIS settings for varia-capacitor characterizations.

SPEIS<sub>7MHz-1Hz</sub> and SPEIS<sub>323kHz</sub>.  $C_1$  and  $C_p$  lead to similar value around 140 pF at low voltage and 20 pF at high voltage. So, the comparison shows that the  $C_1$  calculated with Zfit and  $C_p$  determined directly in the EIS technique are identical.

These values are in agreement with the specification described in the datasheet of the varia-capacitor.

Moreover, SPEIS<sub>7MHz-1Hz</sub> and SPEIS<sub>323kHz</sub> last 6 200 s and 150 s, respectively. So it is possible to save time by performing SPEIS at one frequency.

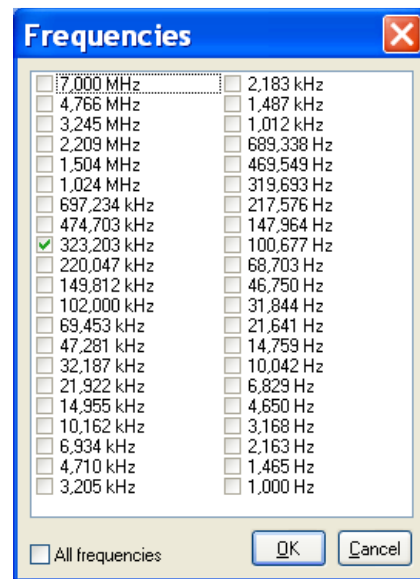


Fig. 7: Frequency selection.

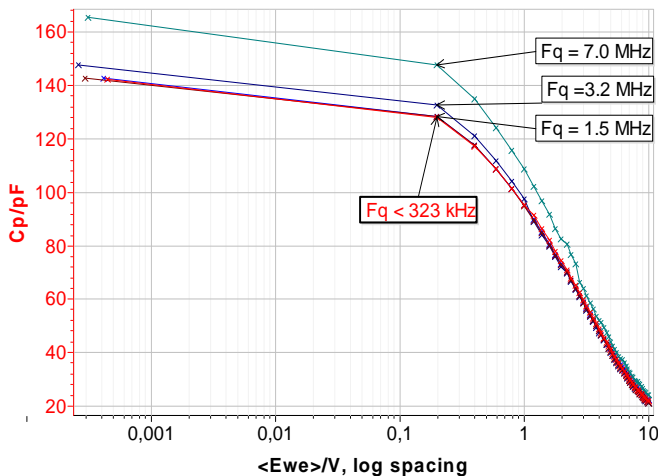


Fig. 6: C-V characterization at different frequencies.

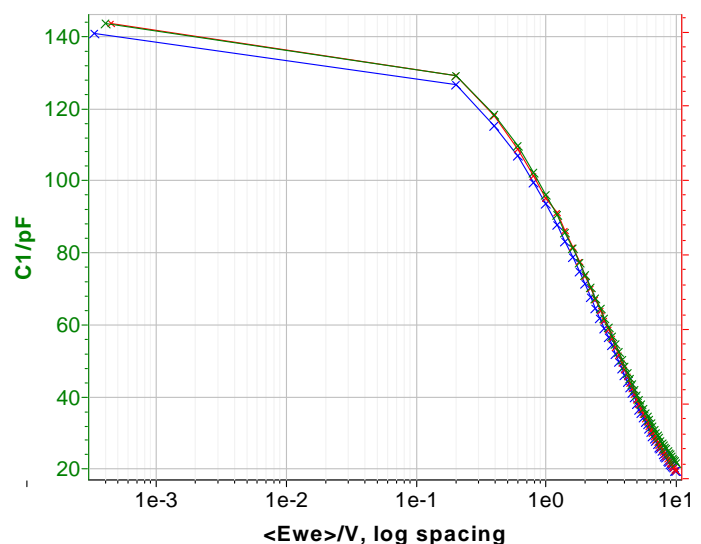


Fig. 8: semi logarithmic C-V curves of varia capacitor.  $C_p$  vs E of SPEIS<sub>323kHz</sub>;  $C_p$  vs E of SPEIS<sub>7MHz-1Hz</sub> and  $C_1$  (from Zfit) vs E of SPEIS<sub>7MHz-1Hz</sub>.

The SPEIS<sub>7MHz-1Hz</sub> allows user to fit the capacitance value,  $C_1$  with the Zfit tool at the different frequencies (window of frequency selection is displayed in Fig. 7).  $C_1$  is compared in Fig. 8 to the value of  $C_p$  that is already calculated during the experiments

## IV- C-V curve of photovoltaic cell

For the PV cell characterization, the voltage is scanned between 3 and 7.5 V and the frequency of the signal is 100 kHz (Fig. 9). According to the application note #24 [1], R/C model is considered. So  $C_p$  vs  $V$  curve is plotted (Fig. 10).

The C-V curve exhibits 3 regions:

- $E < 4V$ : accumulation region
- $4V < E < 6V$ : depletion region
- $E > 6V$ : Inversion region

Fig. 9: C-V curves settings of PV cell characterization.

The doping concentration  $N$  can be determined thanks to the following relationship:

$$N = \frac{2}{e \varepsilon \varepsilon_0 A^2 \left( \frac{d}{dE} \left( \frac{1}{C^2} \right) \right)}$$

Where  $e$  is the electron charge ( $1.60 \times 10^{-19}$  C)  
 $\varepsilon \varepsilon_0$  is the semiconductor permittivity ( $1.03 \times 10^{-12}$  F/cm for silicon)  
 $A$  is the surface of the photovoltaic cell,  $21 \text{ cm}^2$   
 $C$  is the capacitance (F) and  $E$  the voltage (V).

As  $C^{-2}$  variable is also available in the list of available variable (Fig. 1), it is also possible to plot  $C^{-2}$  vs  $E$ . The slope of this curve leads to the doping concentration.

In this case, the slope (determined by linear fit) is  $3.53 \times 10^{15}$  F/V, so the doping concentration is  $1.64 \times 10^{14} \text{ cm}^{-3}$ . This value is in agreement with the values given in the literature [1].

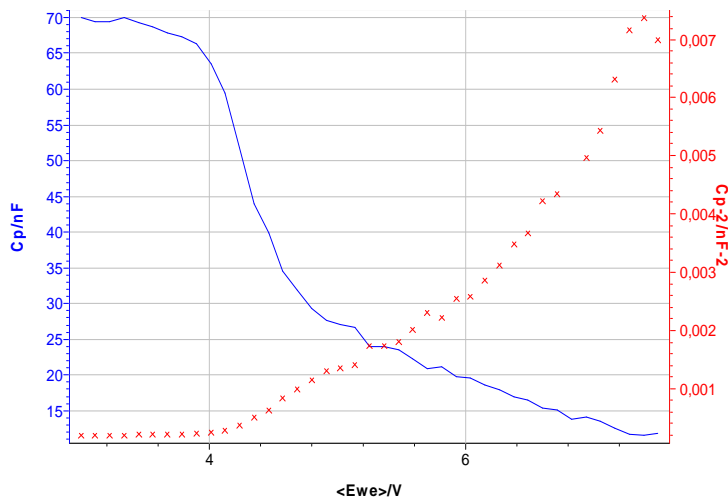


Fig. 10: C-V curves of photovoltaic cell.  $C_p$  vs  $E$  and  $C_p^{-2}$  vs  $E$ .

## IV- Conclusion

The note shows how to perform capacitance measurement without any fitting process. Several advantages:

- Quick measurement, only one frequency is needed to determine  $C_p$  or  $C_s$ . No need of the full EIS spectra.
- No post-treatment: no impedance fitting process is needed
- The graphic package of EC-Lab allows one to plot different types of graph such as  $C$  vs  $E$  in log spacing,  $C^{-2}$  vs  $E$ , and even more...
- It is possible to follow up the capacitance change that can be carried out with the PEISW technique. This technique is also of interest for sensor applications.

## References

[1] Photovoltaic Characterizations: Polarization and Mott Schottky plot, Application Note #24, <http://www.bio-logic.info/potentiostat/notes.html>