

## Application of the Capacitance-Voltage curve to photovoltaic cell characterizations

### I – INTRODUCTION

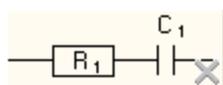
Capacitance measurement is widely used to carry out semiconductor characterization such as photovoltaic (PV) cells. For example, this measurement is used to determine the doping concentration.

In EC-Lab® & EC-Lab® Express software, it is possible to directly plot the capacitance (directly means without any post-process). The capacitance can be obtained with all the Electrochemical Impedance Spectroscopy (EIS) techniques *i.e.* Potentio EIS (PEIS), Galvano EIS (GEIS), Staircase PEIS (SPEIS), Staircase GEIS (SGEIS), “Wait” technique that allows user to follow up the modulus of Z vs time (PEISW) techniques.

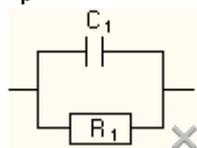
Depending on the model circuits considered, two types of capacitance,  $C_s$  or  $C_p$ , are calculated. The capacitance  $C_s$  corresponds to the capacitance of the R+C (in series) circuit and  $C_p$  corresponds to the capacitance of the R/C (in parallel) circuit (Fig. 1)

	X	Y1	Y2
freq/Hz	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Re[Z]/Ohm	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
-Im[Z]/Ohm	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Z /Ohm	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Phase[Z]/deg	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
time/s	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<Ewe>/V	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<I>/mA	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<b>Cs</b> /μF	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Cs-2/μF-2	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<b>Cp</b> /μF	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Cp-2/μF-2	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
cycle number	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

**C<sub>s</sub>:**



**C<sub>p</sub>:**



**Figure 1: The two equivalent circuits offered for direct capacitance plotting.**

<sup>1</sup> capacitor whose capacitance may be intentionally and repeatedly changed mechanically or electronically

This note exhibits how to plot Capacitance vs. Voltage (C-V) curve. Firstly, the different options offered to plot the capacitance are shown with a varia-capacitor<sup>1</sup> as an experimental model system. Selection of the circuit model and comparison between values of capacitance fitted with Zfit and the capacitance directly available in the technique are discussed. Secondly, typical C-V characterizations of PV cell are described.

### II – EXPERIMENTAL CONDITIONS

Investigations are carried out with a SP-200 equipped with the Ultra Low Current option or with SP-300 and EC-Lab® software. For both systems (*i.e.* varia-capacitor and photovoltaic cell), investigations are done with a standard two-electrode connection.

The characteristic of the varia-capacitor is the following:

- low voltage variable capacitance double diode (BB201 from NXP).
- The capacitance is in the range of 10 to 120 pF for a voltage range of 0.5 to 11V.

The C-V characterization of the PV cell has been performed on a cell irradiated by a Xenon lamp of 150 W (light source of MOS-200 powered by ALX-150 power supply).

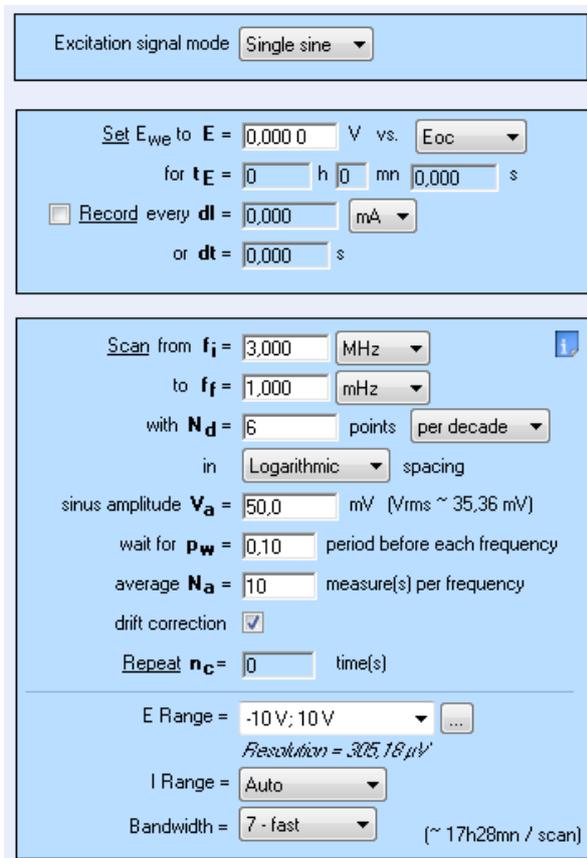
### III – VARIA-CAPACITOR INVESTIGATIONS

#### III - 1 R/C OR R+C EQUIVALENT CIRCUIT?

To choose the appropriate equivalent circuit among R/C or R+C, an EIS measurement on a wide frequency range *i.e.* 3 MHz to 1 mHz is performed. Settings are displayed in Fig. 2.

The EIS measurement leads to a semicircle (Fig. 3), so the R/C model ( $C_p$  variable) is considered for the C-V investigations. The

fitted values of R and C are 70 Ohm and 145 pF (Fig. 4), respectively.



Excitation signal mode: Single sine

Set  $E_{we}$  to  $E = 0,0000$  V vs.  $E_{oc}$

for  $t_E = 0$  h  $0$  mn  $0,000$  s

Record every  $dI = 0,000$  mA

or  $dt = 0,000$  s

Scan from  $f_i = 3,000$  MHz

to  $f_f = 1,000$  mHz

with  $N_d = 6$  points per decade

in Logarithmic spacing

sinus amplitude  $V_a = 50,0$  mV ( $V_{rms} \sim 35,36$  mV)

wait for  $p_w = 0,10$  period before each frequency

average  $N_a = 10$  measure(s) per frequency

drift correction

Repeat  $n_c = 0$  time(s)

E Range = -10 V; 10 V  
*Resolution = 305,18  $\mu$ V*

I Range = Auto

Bandwidth = 7 - fast (~ 17h28mn / scan)

Figure 2: Settings for the EIS characterizations of the varia-capacitor.

### III - 2 C-V INVESTIGATIONS

Two SPEIS techniques are performed. One in the frequency range from 7 MHz to 1 Hz (setting displayed in Fig. 5) and one at one frequency (similar settings than shown in Fig. 5 with  $f_i$  equal to  $f_f$ ). Measurements are performed at a frequency of 323 kHz because above this frequency the responses of the varia-capacitor is dependent on the frequency (Fig. 6). The experiments are named SPEIS<sub>7MHz-1Hz</sub> and SPEIS<sub>323kHz</sub>, respectively. The voltage scan starts at 0V and goes up to 10V with steps of 200 mV.

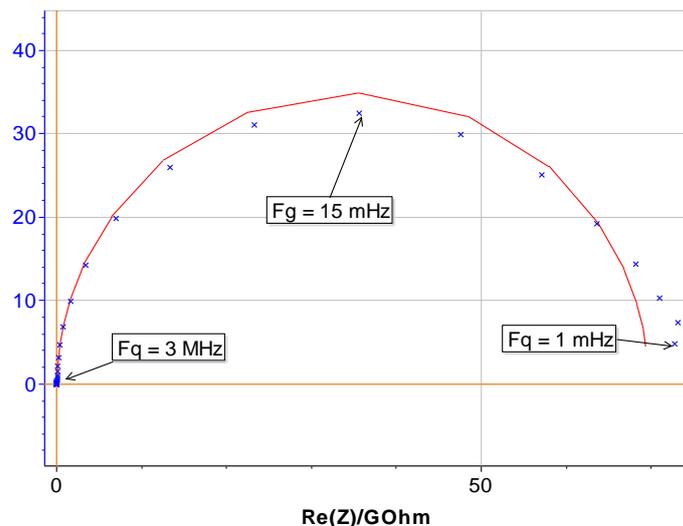
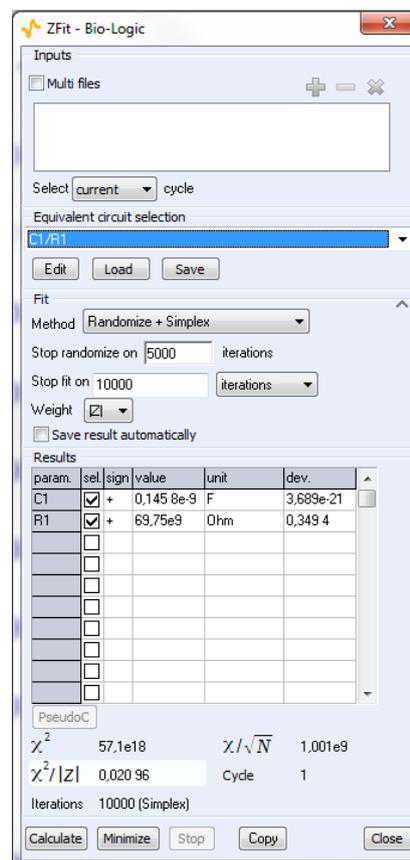


Figure 3: Nyquist plot of varia-capacitor (Exp data fitted data).



ZFit - Bio-Logic

Inputs

Multi files

Select current cycle

Equivalent circuit selection: C1/R1

Fit Method: Randomize + Simplex

Stop randomize on 5000 iterations

Stop fit on 10000 iterations

Weight: |Z|

Save result automatically

param.	sel	sign	value	unit	dev.
C1	<input checked="" type="checkbox"/>	+	0,145 8e-9	F	3,689e-21
R1	<input checked="" type="checkbox"/>	+	69,75e9	Ohm	0,349 4
	<input type="checkbox"/>				
	<input type="checkbox"/>				
	<input type="checkbox"/>				
	<input type="checkbox"/>				
	<input type="checkbox"/>				
	<input type="checkbox"/>				
	<input type="checkbox"/>				

PseudoC

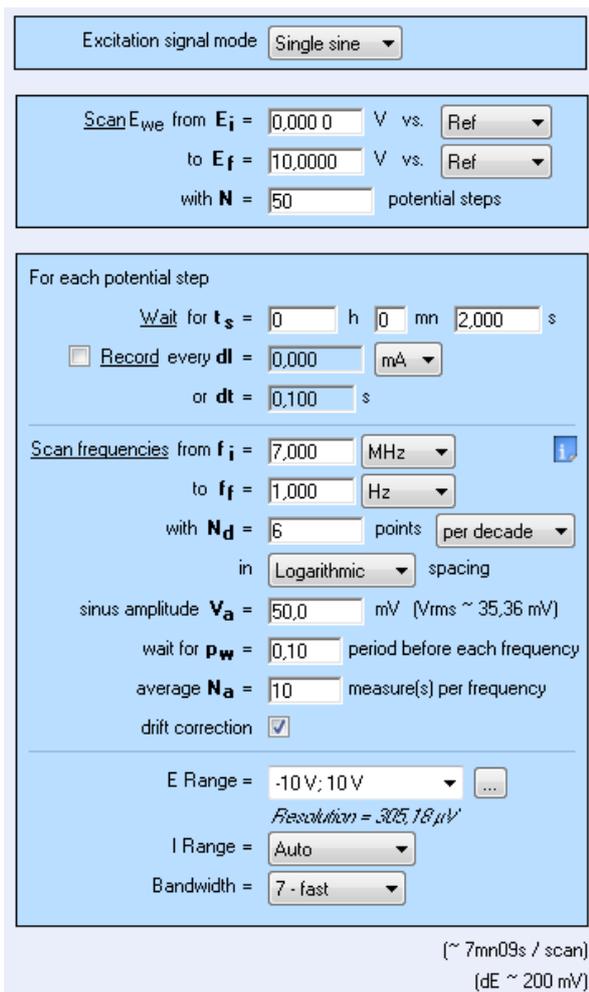
$\chi^2$  57,1e18  $\chi/\sqrt{N}$  1,001e9

$\chi^2/|Z|$  0,020 96 Cycle 1

Iterations 10000 (Simplex)

Buttons: Calculate, Minimize, Stop, Copy, Close

Figure 4: Values of the Zfit process.



Excitation signal mode: Single sine

Scan  $E_{we}$  from  $E_i = 0,0000$  V vs. Ref to  $E_f = 10,0000$  V vs. Ref with  $N = 50$  potential steps

For each potential step

Wait for  $t_s = 0$  h  $0$  mn  $2,000$  s

Record every  $dI = 0,000$  mA or  $dt = 0,100$  s

Scan frequencies from  $f_i = 7,000$  MHz to  $f_f = 1,000$  Hz with  $N_d = 6$  points per decade in Logarithmic spacing

sinus amplitude  $V_a = 50,0$  mV ( $V_{rms} \sim 35,36$  mV)

wait for  $p_w = 0,10$  period before each frequency

average  $N_a = 10$  measure(s) per frequency

drift correction

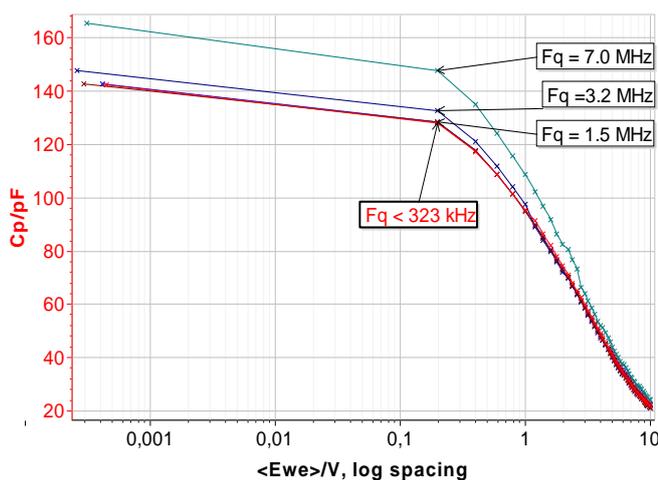
E Range = -10 V; 10 V Resolution = 305,18  $\mu$ V

I Range = Auto

Bandwidth = 7 - fast

(~ 7mn09s / scan)  
(dE ~ 200 mV)

**Figure 5: SPEIS settings for varia-capacitor characterizations.**



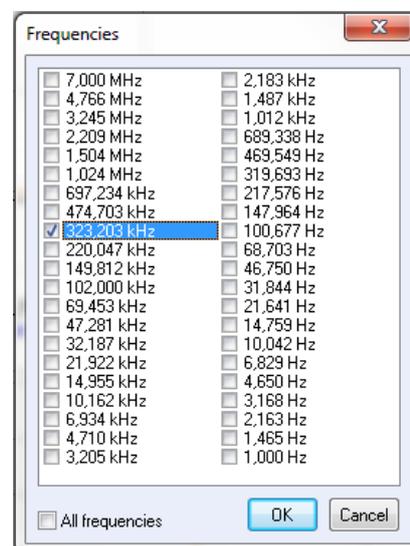
**Figure 6: C-V characterization at different frequencies.**

The SPEIS<sub>7MHz-1Hz</sub> allows user to fit the capacitance value,  $C_1$  with the Zfit tool at the different frequencies (window of frequency selection is displayed in Fig. 7).  $C_1$  is compared in Fig. 8 to the value of  $C_p$  that is already

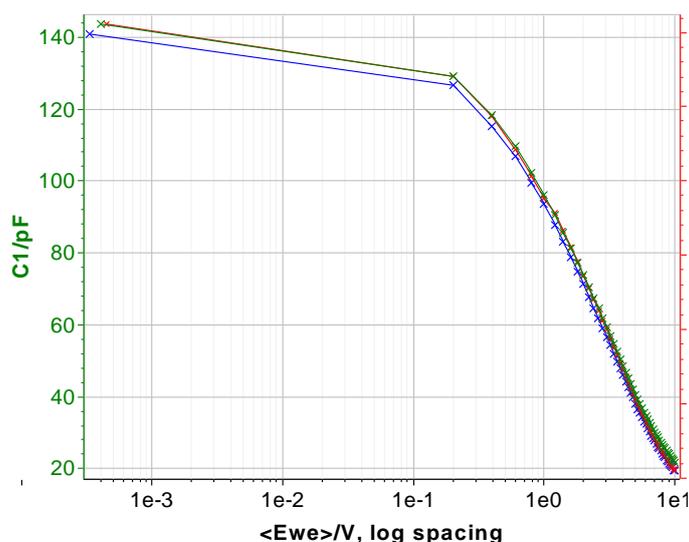
calculated during the experiments SPEIS<sub>7MHz-1Hz</sub> and SPEIS<sub>323kHz</sub>.  $C_1$  and  $C_p$  lead to similar value around 140 pF at low voltage and 20 pF at high voltage. So, the comparison shows that the  $C_1$  calculated with Zfit and  $C_p$  determined directly in the EIS technique are identical.

These values are in agreement with the specification described in the datasheet of the varia-capacitor.

Moreover, SPEIS<sub>7MHz-1Hz</sub> and SPEIS<sub>323kHz</sub> last 6 200 s and 150 s, respectively. So it is possible to save time by performing SPEIS at one frequency.



**Figure 7: Frequency selection.**



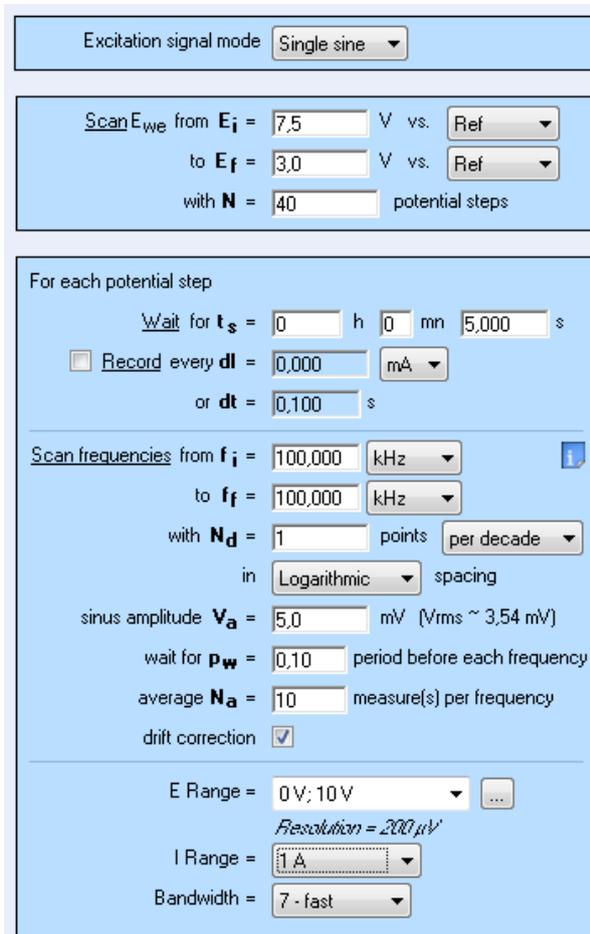
**Figure 8: semi logarithmic C-V curves of varia capacitor.  $C_p$  vs  $E$  of SPEIS<sub>323kHz</sub>;  $C_p$  vs.  $E$  of SPEIS<sub>7MHz-1Hz</sub> and  $C_1$  (from Zfit) vs.  $E$  of SPEIS<sub>7MHz-1Hz</sub>.**

## IV – C-V CURVE OF PHOTOVOLTAIC CELL

For the PV cell characterization, the voltage is scanned between 3 and 7.5 V and the frequency of the signal is 100 kHz (Fig. 9). According to the application note #24 [1], R/C model is considered. So  $C_p$  vs  $V$  curve is plotted (Fig. 10).

The C-V curve exhibits 3 regions:

- $E < 4V$ : accumulation region
- $4V < E < 6V$ : depletion region
- $E > 6V$ : Inversion region



**Figure 9: C-V curves settings of PV cell characterization.**

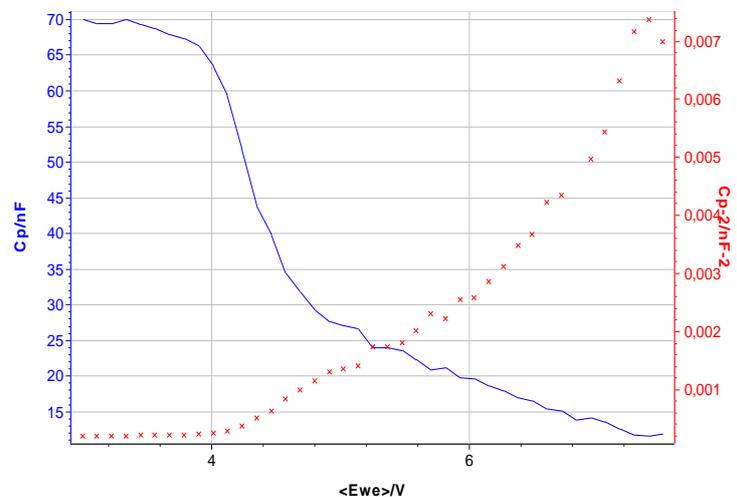
The doping concentration  $N$  can be determined thanks to the following relationship:

$$N = \frac{2}{e\epsilon\epsilon_0 A^2 \left( \frac{d\left(\frac{1}{C^2}\right)}{dE} \right)} \quad (1)$$

Where  $e$  is the electron charge ( $1.60 \times 10^{-19}$  C)  
 $\epsilon_0$  is the semiconductor permittivity ( $1.03 \times 10^{-12}$  F/cm for silicon)  
 $A$  is the surface of the photovoltaic cell,  $21 \text{ cm}^2$   
 $C$  is the capacitance (F) and  $E$  the voltage (V).

As  $C^2$  variable is also available in the list of available variable (Fig. 1), it is also possible to plot  $C^2$  vs.  $E$ . The slope of this curve leads to the doping concentration.

In this case, the slope (determined by linear fit) is  $3.53 \times 10^{15}$  F/V, so the doping concentration is  $1.64 \times 10^{14} \text{ cm}^{-3}$ . This value is in agreement with a value previously given [1].



**Figure 10: C-V curves of photovoltaic cell.  $C_p$  vs.  $E$  and  $C_p^2$  vs.  $E$ .**

## IV – CONCLUSION

The note shows how to perform capacitance measurement without any fitting process. Several advantages:

- Quick measurement, only one frequency is needed to determine  $C_p$  or  $C_s$ . No need of the full EIS spectra.
- No post-treatment: no impedance fitting process is needed

- The graphic package of EC-Lab allows one to plot different types of graph such as  $C$  vs.  $E$  in log spacing,  $C^2$  vs.  $E$ , and even more... It is possible to follow up the capacitance change that can be carried out with the PEISW technique. This technique is also of interest for sensor applications.

*Data files can be found in :*

*C:\Users\xxx\Documents\EC-Lab\Data\Samples\Photovoltaic\X\_C\_V\_Character*

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## REFERENCES

- 1) [Application Note #24](#) “Photovoltaic Characterizations: Polarization and Mott-Schottky plot”

*Revised in 07/2018*